

SECTION AND MIDPOINT FORMULA AND EQUATION OF LINE

- 1) In what ratio does the point $M(p, -1)$ divide the line segment joining the points $A(1, -3)$ and $B(6, 2)$? Hence find the value of p .
- 2) $A(-4, 4)$, $B(X, -1)$ and $C(6, Y)$ are the vertices of triangle ABC . If the centroid of this triangle ABC is at the origin, find the values of X and Y .
- 3) $A(2, 5)$, $B(-1, 2)$, and $C(5, 8)$ are the vertices of triangle ABC . P and Q are points on AB and AC respectively such that $AP:PB = AQ:QC = 1:2$.
(a) Find the co-ordinates of points P and Q (b) show that $BC = 3 \cdot PQ$
- 4) show that the points (a, b) , $(a+3, b+4)$, $(a-1, b+7)$ and $(a-4, b+3)$ are the vertices of a parallelogram.
- 5) what point on x -axis is equidistant from the points $(6, 7)$ and $(4, -3)$?
- 6) In general point on y -axis is represented as -----
- 7) In general point on x -axis is represented as -----
- 8) EQUATION parallel to x -axis is -----
- 9) Equation parallel to y -axis is -----
- 10) Find the ratio in which the line $2x+3y-5=0$ divides the line segment joining the points $(8, -9)$ and $(2, 1)$. Also, find the co-ordinates of the point of division.
- 11) if the mid point of the line segment joining the points $A(3, 4)$, $(k, 6)$ is $P(x, y)$ and $x+y-10=0$, find the value of k .
- 12) Find the co-ordinates of the point Q on x -axis which lies on the perpendicular bisector of the line segment joining the points $A(-5, -2)$ and $B(4, 2)$. Name the type of the triangle QAB .
- 13) Find the co-ordinates of the circumcenter of the triangle whose vertices are $(3, 0)$, $(-1, -6)$ and $(4, -1)$. Also find its circumradius.

14) Find the ratio in which the two co-ordinate axes divide the line segment joining the points $(-2,5)$ and $(1,-9)$.

15) The point P divides the join of $(2,1)$ and $(-3,6)$ in the ratio $2:3$. Does P lie on the line $x-5y+15=0$?

16) If $P(9a-2, -b)$ divides the line segment joining the points $A(3a+1, -3)$ and $B(8a, 5)$ in the ratio $3:1$. Find the values of a and b .

17) $P(1, -2)$ is a point on the line segment AB such that $AP:PB$ is equal to $2:3$. Find the co-ordinates of B .

18) Prove that the points A(-5,4) B(-1,-2) and C(5,2) are the vertices of an isosceles right angled triangle. Find the co-ordinates of D so that ABCD is a square.

19) The line joining the points (2,-1) and (5,-8) is trisected at the points P and Q. If point P lies on the line $2x-y+k=0$, find the value of k. Also find the co-ordinates of point Q.

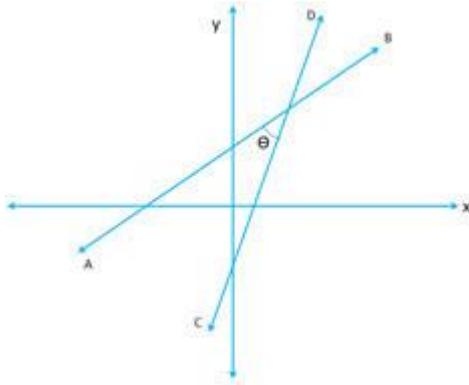
20) A(20,0) and B(10,-20) are two fixed points. Find the co-ordinates of the point P in AB such that $3PB=AB$. Also, find the co-ordinates of some other point Q in AB such that $AB=6AQ$.

Equation of Line:

Question 1: A line intersects x -axis at point $(-2, 0)$ and cuts off an intercept of 3 units from the positive side of y -axis. Find the equation of the line.

Question 2: Find the equation of a line passing through the point $(2, 3)$ and having the x -intercept of 4 units.

Question 3: The given figure (not drawn to scale) shows two straight lines AB and CD . If equation of the line AB is $y = x + 1$ and equation of CD is $y = \sqrt{3}x - 1$. Write down the inclination of lines AB and CD ; also, find the angle between AB and CD .



Question 4: Write down the equation of the line whose gradient is $\frac{2}{3}$ and which passes through P , where P divides the line segment joining $A(-2, 6)$ and $B(3, -4)$ in the ratio $2 : 3$

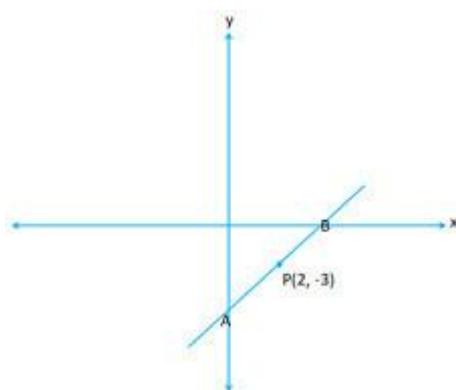
Question 5: Point A and B have co-ordinates $(7, 3)$ and $(1, 9)$ respectively. Find:

(i) The slope of AB

(ii) The equation of perpendicular bisector of the line segment AB

(iii) The value of p if $(-2, p)$ lies on it

Question 6: A and B are two points on the x -axis and y -axis respectively. $P(2, -3)$ is the mid-point of AB . Find the



(i) Co-ordinates of A and B

(ii) Slope of line AB

(iii) Equation of line AB

Question 7: The equation of a line is $3x + 4y - 7 = 0$. Find:

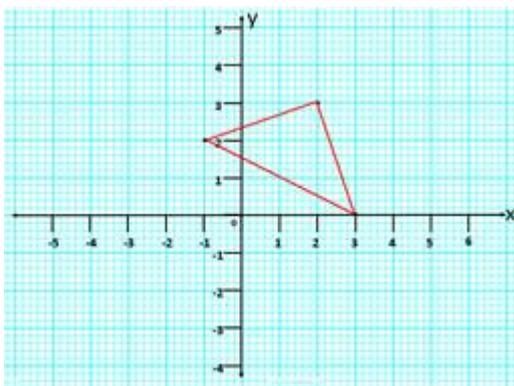
(i) Slope of the line.

(ii) The equation of a line perpendicular to the given line and passing through the intersection of the lines $x - y + 2 = 0$ and $3x + y - 10 = 0$

Question 8: $ABCD$ is a parallelogram where $A(x, y)$, $B(5, 8)$, $C(4, 7)$ and $D(2, -4)$. Find:

(i) Co-ordinates of A

(ii) Equation of diagonal BD



Question 9: From the given figure, find:

(i) The co-ordinates of $A, B,$ and C .

(ii) The equation of the line through A and parallel to BC .

Question 10: $P(3, 4), Q(7, -2)$ and $R(-2, -1)$ are the vertices of triangle PQR . Write down the equation of the median of the triangle through R .

Question 11: Find the value of k for which the lines $kx - 5y + 4 = 0$ and $5x - 2y + 5 = 0$ are perpendicular to each other.

Question 12: A straight line passes through the points $P(-1, 4)$ and $Q(5, -2)$. It intersects the co-ordinate axes at points A and B . M is the mid-point of the line segment AB . Find:

- The equation of line
- The co-ordinates of A and B
- The co-ordinates of M

Question 13: If the lines $y = 3x + 7$ and $2y + px = 3$ are perpendicular to each other, find the value of p .

Question 14: The line through $A(-2, 3)$ and $B(4, b)$ is perpendicular to the line $2x - 4y = 5$. Find the value of b

Question 15: i) Find the equation of the line passing through $(5, -3)$ and

parallel to $x - 3y = 4$.

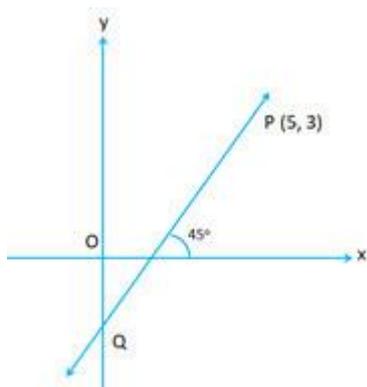
ii) Find the equation of the line parallel to the line $3x + 2y = 8$ and passing through the point $(0, 1)$

Question 16: i) Write down the equation of the line AB , through $(3, 2)$ and perpendicular to the line $2y = 3x + 5$.

ii) AB meets the x - axis at A and the y - axis at B . write down the coordinates of A and B . Calculate the area of triangle OAB , where O is origin.

Question 17: Find the value of a for the points $A(a, 3)$, $B(2, 1)$ and $C(5, a)$ are collinear. Hence, find the equation of the line.

Question 18: In, $A = (3, 5)$, $B = (7, 8)$ and $C = (1, -10)$. Find the equation of the median through A .



Question 19: The line through $P(5, 3)$ intersects y - axis at Q .

i) Write the slope of the line.

ii) Write the equation of the line.

iii) Find the co-ordinates of Q

Question 20: $A(1, 4)$, $B(3, 2)$ and $C(7, 5)$ are vertices of a triangle ABC .

Find:

i) The co-ordinates of the centroid of a triangle ABC .

ii) The equation of a line through the centroid and parallel to AB .