

VAGDEVI VILAS SCHOOL-MARATHAHALLI

MID TERM EXAMINATION(2019-20)

MATHEMATICS

STD: X

MAX MARKS:80

DATE:23/09/2019

DURATION: 3 Hrs

General Instructions:

- i) All questions are compulsory.
- ii) The question paper consists of 40 questions divided into four sections- A,B,C and D
- iii) Section – A Questions 1 – 20 carry 1 mark each.
- iv) Section – B Questions 21 – 26 carry 2 marks each.
- v) Section – C Questions 27 – 34 carry 3 marks each.
- vi) Section – D Questions 35 – 40 carry 4 marks each.
- vii) There is no overall choice. However, an internal choice has been provided in two questions of two marks each, two questions of three marks each, three questions of four marks each. You have to attempt only one of the alternatives in all such questions.
- viii) Use of calculators is not permitted

SECTION-A

1. The decimal expansion of $14753/1250$ will terminate after how many decimal places?
a) 1 b) 2 c) 3 d) 4
2. For positive integers "a" and 4, there exist unique integers q and r such that $a=4q+r$ where r must satisfy:
a) $0 \leq r < 4$ b) $1 \leq r < 4$ c) $0 < r < 4$ d) $0 \leq r \leq 4$
3. A cubic polynomial can have _____ zeroes.
a) exactly 3 zeroes b) at least 3 zeroes c) at most 3 zeroes d) no zeroes
4. A quadratic polynomial whose zeroes are -5 and 3 is _____
a) $x^2 - 2x - 15$ b) $x^2 - 2x + 15$ c) $x^2 + 2x + 15$ d) $x^2 + 2x - 15$

5. If a pair of linear equations is inconsistent then their graph lines will be _____
- a) parallel b) intersecting lines
c) coincident d) intersecting or coincident
6. A line that intersects a circle at two distinct points is _____
- a) tangent b) secant c) chord d) diameter
7. Which of the following pairs of lines in a circle cannot be parallel?
- a) two chords b) a chord and a tangent c) two tangents d) two diameters
8. Corresponding sides of two similar triangles are in the ratio 4:9, Areas of these triangles are in the ratio
- a) 2:3 b) 4:9 c) 9:4 d) 16:81
9. A man goes 10m due east and then 20m due north .His distance from the starting point is _____
- a) $10\sqrt{5}$ b) 10 c) $5\sqrt{10}$ d) 5
10. L.C.M of $5^2 \times 3^3$ and $3^2 \times 5^3$ is _____
- a) $5^2 \times 3^2$ b) $5^3 \times 3^3$ c) $5^2 \times 3^3$ d) $5^3 \times 3^2$
11. If $\sqrt{3} \tan 2\theta - 3 = 0$ then $\theta =$ _____
- a) 15° b) 30° c) 45° d) 60°
12. $3 \cos^2 60^\circ + 2 \cot^2 30^\circ - 5 \sin^2 45^\circ =$ _____
- a) $13/6$ b) $17/4$ c) 1 d) 4
13. If the product of the roots of the equation $x^2 - 3x + k = 10$ is -2 then the value of k is _____
- a) -2 b) -8 c) 8 d) 12
14. In a lottery there are 8 prizes and 16 blanks. What is the probability of getting a prize?
- a) $1/2$ b) $1/3$ c) $2/3$ d) $3/2$

15. If $P(a/2, 4)$ is the midpoint of the line segment joining the points $A(-6, 5)$ and $B(-2, 3)$ then the value of 'a' is _____

- a) -8 b) 3 c) -4 d) 4

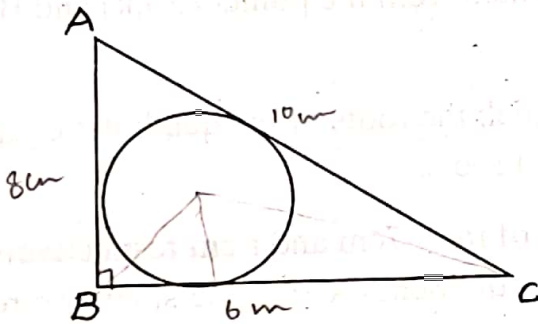
16. A pole 6m high casts a shadow $2\sqrt{3}$ m long on the ground then the sun's elevation is _____

- a) 60° b) 45° c) 30° d) 90°

17. The perimeter of a triangle with vertices $(0, 4), (0, 0), (3, 0)$ is

- a) 5 b) 12 c) 7 d) $7 + \sqrt{3}$

18. In the figure ABC is a right triangle with $\angle ABC = 90^\circ$. If $BC = 6$ cm and $AB = 8$ cm then the radius of its incircle is _____



- a) 1cm b) 2cm c) 3cm d) 4cm

19. The perimeter of a rectangle is 82m and its area is 400m^2 . The breadth of the rectangle is _____

- a) 25m b) 20m c) 16m d) 9m

20. From a point A 10cm away from the centre of a circle a tangent AT of length 8cm is drawn, then the radius of the circle is _____

- a) 12 cm b) 10cm c) 8cm d) 6cm

SECTION -B

21. Find the HCF and LCM of 180 and 288 by prime factorization method.
22. Divide the polynomial $p(x) = x^4 - 3x^2 + 4x + 5$ by $g(x) = x^2 + 1 - x$ and find the quotient and the remainder

Or

If α and β are the zeros of the quadratic polynomial $f(x) = x^2 - x - 2$ find a polynomial whose zeros are $2\alpha + 1$ and $2\beta + 1$

23. If $\sec 4A = \operatorname{cosec} (A - 20^\circ)$ where $4A$ is an acute angle, find the value of A
24. Find the ratio in which the line segment AB (-6, 10) and B (3, -8) is divided by (-4, 6)

Or

If the point $P(k-1, 2)$ is equidistant from the points $A(3, k)$ and $B(k, 5)$, find the values of k .

25. Find the values of k for which the roots of the quadratic equation $2x^2 + kx + 8 = 0$ will have equal roots.

26. Two concentric circles are of radii 7cm and r cm respectively, where $r > 7$, a chord of the larger circle of length 48cm touches the smaller circle. Find the value of r

SECTION -C

27. Solve $8x + 5y = 9$ and $3x + 2y = 4$ by elimination method.

28. A plane left 30 minutes later than the schedule time and in order to reach its destination 1500km away in time it has to increase its speed by 250km/hr. from its usual speed. Find its usual speed.

29. If BL and CM are medians of a triangle ABC right angled at A then prove that $4(BL^2 + CM^2) = 5 BC^2$

Or

In an equilateral triangle ABC, D is a point on side BC such that $BD = BC/3$. Prove that $9AD^2 = 7 AB^2$

30. Prove the following:

i) $(\sin\theta + \operatorname{cosec}\theta)^2 + (\cos\theta + \sec\theta)^2 = 7 + \tan^2\theta + \cot^2\theta$

ii) $\sqrt{\frac{1 + \sin\theta}{1 - \sin\theta}} = \sec\theta + \tan\theta$

31. Prove that a parallelogram circumscribing a circle is a rhombus

Or

Prove that opposite sides of a quadrilateral circumscribing a circle subtend supplementary angles at the Centre of the circle.

32. Prove that the lengths of tangents drawn from an external point to a circle are equal.

33. A motor boat whose speed is 18km/hr in still water takes 1 hr more to go 24km upstream than to return downstream to the same spot. Find the speed of the stream.

34. The probability of selecting a red ball at random from a jar that contains only red, blue and orange balls is $\frac{1}{4}$. The probability of selecting a blue ball at random from the same jar is $\frac{1}{3}$. If the jar contains 10 orange balls, find the total number of balls in the jar.

SECTION-D

35. Prove that $15 + 11\sqrt{3}$ is an irrational number.

Or

If the H.C.F of 152 and 272 is expressible in the form $272 X 8 + 152x$, then find x

36. Find all the zeros of the polynomial $2x^4 + 7x^3 - 19x^2 - 14x + 30$, if two of its zeros are $\sqrt{2}$ and $-\sqrt{2}$

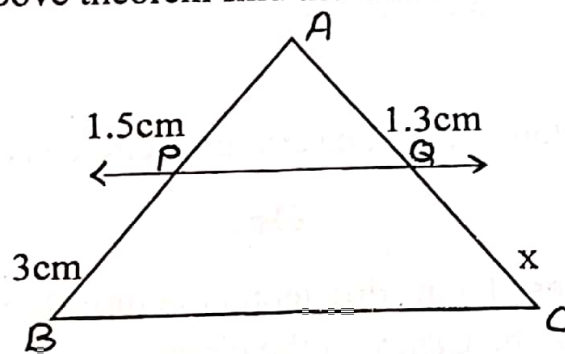
Or

Find all the zeros of the polynomial $x^4 - 3x^3 - x^2 + 9x - 6$, if two of its zeros are $\sqrt{3}$ and $-\sqrt{3}$

37. Solve the pair of linear equations graphically $x - y = 1$, $2x + y = 8$, shade the area bounded by these two lines and y-axis, also determine this area

38. i) State and prove Basic proportionality theorem.

ii) Using the above theorem find the value of x if $PQ \parallel BC$



Or

i) State and prove the Pythagoras theorem.

ii) A ladder 10m long reaches a window 8m above the ground. Find the distance of the foot of the ladder from base of the wall.

39. If the points $A(1, 2)$, $B(2, 1)$, $C(-3, 2)$ and $D(-4, -3)$ are the vertices of the parallelogram ABCD then taking AB as the base, find the height of the parallelogram. (area)

40. A card is drawn at random from a well shuffled deck of playing cards. Find the probability that the card drawn is

i) a king or a jack

ii) a red card

iii) a black queen

iv) a face card